# University of North Carolinat Charlotte Department of Electrical and Computer Engineering 

## Experiment 1 - MAXIMUM Power transfer

## ObJECTIVES

In this experiment the student will investigate the circuit requirements for the transfer of maximum power from the power source to the load in DC circuits with only real impedances.

## MATERIALS/EQUIPMENT NEEDED

DC Voltage Source (capable of 10 Vdc )
Resistors: $100 \Omega, 1 \mathrm{k} \Omega, 10 \mathrm{k} \Omega, 100 \mathrm{k} \Omega$
Decade Resistor Box
Multimeter

## INTRODUCTION

The circuit shown in Figure 1-1 uses an ideal voltage source in series with a sourcing resistance to approximate a practical voltage source in which the terminal voltage drops with increasing load current. In a resistive circuit like this, the resistive load receives maximum power when the load resistance is equal to the source resistance $\left(\mathrm{R}_{\mathrm{L}}=\mathrm{R}_{\mathrm{s}}\right)$. The maximum power can be calculated using the expression

$$
p_{\max }=\frac{V_{s}^{2}}{4 R_{s}}
$$

The laboratory experiment will verify, for several sourcing resistors, that maximum power transfer is achieved when the load resistance is selected as established above.


Figure 1-1 Lab circuit setup

## Prelab

1. For the circuit shown in Figure 1-1, determine the theoretical value of the load voltage and load power for a $100 \Omega$ source resistance and load resistances in Table 1-1.
2. For the circuit shown in Figure 1-1, determine the theoretical value of the load voltage and load power for a $1 \mathrm{k} \Omega$ source resistance and load resistances in Table 1-2.
3. For the circuit shown in Figure 1-1, determine the theoretical value of the load voltage and load power for a $10 \mathrm{k} \Omega$ source resistance and load resistances in Table 1-3.
4. For the circuit shown in Figure 1-1, determine the theoretical value of the load voltage and load power for a $100 \mathrm{k} \Omega$ source resistance and load resistances in Table 1-4.

## Procedure

1. Construct the circuit shown in Figure 1-1 using a variable voltage source, a fixed resistor for the sourcing resistance and a decade box for the load resistance.
2. Be careful that your voltage source is set to a value that will not cause the power ratings of the selected sourcing resistor or the decade box to be exceeded.
3. Additionally, the selected decade box must cover the range of values presented in Tables 1-1 to $1-4$ so the plot of power vs. load resistance will show a clear maximum.
4. To determine load power, measure the load voltage and calculate the load power. Complete these measurements and calculations for sourcing resistances of $100 \Omega, 1 \mathrm{k} \Omega, 10 \mathrm{k} \Omega$, and $100 \mathrm{k} \Omega$. Record your results in the tables.

## DATA/OBSERVATIONS

Table 1-1: Values for $100 \Omega$ Source Resistance and Variable Load Resistance

| Rs | $\mathbf{R}_{\mathbf{L}}$ | Theoretical |  | Measurements |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | VL | $\begin{gathered} \mathbf{P}_{\mathrm{L}}= \\ \left(\mathbf{V}_{\mathrm{L}}\right)^{2} / \mathbf{R}_{\mathrm{L}} \end{gathered}$ | VL | $\begin{gathered} \mathbf{P}_{\mathrm{L}}= \\ \left(\mathbf{V}_{\mathrm{L}}\right)^{2} / \mathbf{R}_{\mathrm{L}} \end{gathered}$ |
| $100 \Omega$ | 10 |  |  |  |  |
|  | 50 |  |  |  |  |
|  | 75 |  |  |  |  |
|  | 90 |  |  |  |  |
|  | 95 |  |  |  |  |
|  | 100 |  |  |  |  |
|  | 105 |  |  |  |  |
|  | 110 |  |  |  |  |
|  | 125 |  |  |  |  |
|  | 500 |  |  |  |  |
|  | 1K |  |  |  |  |
|  | 5K |  |  |  |  |
|  | 10K |  |  |  |  |
|  | 50K |  |  |  |  |
|  | 75K |  |  |  |  |
|  | 100K |  |  |  |  |

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Table 1-2: Values for $1 \mathrm{~K} \Omega$ Source Resistance and Variable Load Resistance

| Rs | RL | Theoretical |  | Measured |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | VL | $\begin{gathered} \mathbf{P}_{\mathrm{L}}= \\ \left(\mathbf{V}_{\mathrm{L}}\right)^{2} / \mathbf{R}_{\mathrm{L}} \end{gathered}$ | VL | $\begin{gathered} \mathbf{P}_{\mathbf{L}}= \\ \left(\mathbf{V}_{\mathrm{L}}\right)^{2} / \mathbf{R}_{\mathrm{L}} \end{gathered}$ |
| 1K $\Omega$ | 10 |  |  |  |  |
|  | 50 |  |  |  |  |
|  | 100 |  |  |  |  |
|  | 500 |  |  |  |  |
|  | 900 |  |  |  |  |
|  | 950 |  |  |  |  |
|  | 975 |  |  |  |  |
|  | 1K |  |  |  |  |
|  | 1.25K |  |  |  |  |
|  | 1.5K |  |  |  |  |
|  | 1.75K |  |  |  |  |
|  | 5K |  |  |  |  |
|  | 10K |  |  |  |  |
|  | 50K |  |  |  |  |
|  | 75K |  |  |  |  |
|  | 100K |  |  |  |  |

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Table 1-3: Values for $10 \mathrm{~K} \Omega$ Source Resistance and Variable Load Resistance

| Rs | RL | Theoretical |  | Measured |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | VL | $\begin{gathered} \mathbf{P}_{\mathbf{L}}= \\ \left(\mathbf{V}_{\mathrm{L}}\right)^{2} / \mathbf{R}_{\mathrm{L}} \end{gathered}$ | VL | $\begin{gathered} \mathbf{P}_{\mathrm{L}}= \\ \left(\mathbf{V}_{\mathrm{L}}\right)^{2} / \mathbf{R}_{\mathrm{L}} \end{gathered}$ |
| 10K $\Omega$ | 10 |  |  |  |  |
|  | 50 |  |  |  |  |
|  | 100 |  |  |  |  |
|  | 500 |  |  |  |  |
|  | 1K |  |  |  |  |
|  | 5K |  |  |  |  |
|  | 7K |  |  |  |  |
|  | 9K |  |  |  |  |
|  | 9.5K |  |  |  |  |
|  | 9.75K |  |  |  |  |
|  | 10K |  |  |  |  |
|  | 10.25K |  |  |  |  |
|  | 10.5K |  |  |  |  |
|  | 11K |  |  |  |  |
|  | 12K |  |  |  |  |
|  | 25K |  |  |  |  |
|  | 50K |  |  |  |  |
|  | 75K |  |  |  |  |
|  | 100K |  |  |  |  |



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Table 1-4: Values for $100 \mathrm{~K} \Omega$ Source Resistance and Variable Load Resistance

| Rs | $\mathbf{R}_{\mathbf{L}}$ | Theoretical |  | Measurement |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{V}_{\text {L }}$ | $\begin{gathered} \mathbf{P}_{\mathrm{L}}= \\ \left(\mathrm{V}_{\mathrm{L}}\right)^{2} / \mathbf{R}_{\mathrm{L}} \end{gathered}$ | $\mathbf{V}_{\text {L }}$ | $\begin{gathered} \mathbf{P}_{\mathbf{L}}= \\ \left(\mathbf{V}_{\mathbf{L}}\right)^{2} / \mathbf{R}_{\mathbf{L}} \end{gathered}$ |
| $100 \mathrm{~K} \Omega$ | 10 |  |  |  |  |
|  | 50 |  |  |  |  |
|  | 100 |  |  |  |  |
|  | 500 |  |  |  |  |
|  | 1K |  |  |  |  |
|  | 5K |  |  |  |  |
|  | 10K |  |  |  |  |
|  | 50K |  |  |  |  |
|  | 75K |  |  |  |  |
|  | 90K |  |  |  |  |
|  | 95K |  |  |  |  |
|  | 97K |  |  |  |  |
|  | 99K |  |  |  |  |
|  | 100K |  |  |  |  |
|  | 101K |  |  |  |  |
|  | 103K |  |  |  |  |
|  | 105K |  |  |  |  |
|  | 110K |  |  |  |  |

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## Post-LAB

Post-Lab questions must be answered in each experiment's laboratory report.

1. Create Table 1-5 in Excel or similar software for import into your write-up. Use the values from the Pre-Lab to calculate theoretical maximum power.

$$
\% \text { error }=\frac{\text { meas }- \text { theo }}{\text { theo }} \times 100
$$

Table 1-5: Maximum Power Transfer for Source Resistors

| Source <br> Resistance | Load <br> Resistance | Measured <br> Load <br> Voltage <br> $\mathbf{V}_{\mathrm{L}}$ | Maximum <br> Power <br> (Measured) <br> $\mathbf{P}_{\mathrm{L}}$ <br> $=\left(\mathrm{V}_{\mathrm{L}}\right)^{2} / \mathbf{R}_{\mathrm{L}}$ | Maximum <br> Power <br> (Theoretical) <br> $\mathbf{P}=\left(\mathrm{Vs}^{2}\right)^{2} / 4 \mathrm{R}_{\mathrm{s}}$ | Percent <br> Error |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1 0 0 \Omega}$ |  |  |  |  |  |
| $\mathbf{1 0 0 0 \Omega}$ |  |  |  |  |  |
| $\mathbf{1 0 K ~ \Omega}$ |  |  |  |  |  |
| $\mathbf{1 0 0 \mathrm { K } \boldsymbol { \Omega }}$ |  |  |  |  |  |

2. For each of the four sourcing resistors, create a plot of output power vs. load resistance. Format axis to show bell curve.
3. Explain how resistor tolerances can cause errors in the experimentally determined maximum power.

Be sure to include all items from the post-lab exercise above in your written lab report.

